



**University of
Zurich**^{UZH}

**Zurich Open Repository and
Archive**

University of Zurich
University Library
Strickhofstrasse 39
CH-8057 Zurich
www.zora.uzh.ch

Year: 2016

Influence of the exchange and correlation functional on the structure of amorphous InSb and In₃SbTe₂ compounds

Gabardi, Silvia ; Caravati, Sebastiano ; Los, Jan H ; Kühne, Thomas D ; Bernasconi, Marco

Abstract: We have investigated the structural, vibrational, and electronic properties of the amorphous phase of InSb and In₃SbTe₂ compounds of interest for applications in phase change non-volatile memories. Models of the amorphous phase have been generated by quenching from the melt by molecular dynamics simulations based on density functional theory. In particular, we have studied the dependence of the structural properties on the choice of the exchange-correlation functional. It turns out that the use of the Becke-Lee-Yang-Parr functional provides models with a much larger fraction of In atoms in a tetrahedral bonding geometry with respect to previous results obtained with the most commonly used Perdew-Becke-Ernzerhof functional. This outcome is at odd with the properties of Ge₂Sb₂Te₅ phase change compound for which the two exchange-correlation functionals yield very similar results on the structure of the amorphous phase.

DOI: <https://doi.org/10.1063/1.4950817>

Posted at the Zurich Open Repository and Archive, University of Zurich

ZORA URL: <https://doi.org/10.5167/uzh-128650>

Journal Article

Published Version

Originally published at:

Gabardi, Silvia; Caravati, Sebastiano; Los, Jan H; Kühne, Thomas D; Bernasconi, Marco (2016). Influence of the exchange and correlation functional on the structure of amorphous InSb and In₃SbTe₂ compounds. *Journal of Chemical Physics*, 144(20):204508.

DOI: <https://doi.org/10.1063/1.4950817>

Influence of the exchange and correlation functional on the structure of amorphous InSb and In₃SbTe₂ compounds

Silvia Gabardi, Sebastiano Caravati^{*}, Jan H. Los^{*}, Thomas D. Kühne^{*}, and Marco Bernasconi^{*}

Citation: *J. Chem. Phys.* **144**, 204508 (2016); doi: 10.1063/1.4950817

View online: <http://dx.doi.org/10.1063/1.4950817>

View Table of Contents: <http://aip.scitation.org/toc/jcp/144/20>

Published by the [American Institute of Physics](#)

Influence of the exchange and correlation functional on the structure of amorphous InSb and In₃SbTe₂ compounds

Silvia Gabardi,¹ Sebastiano Caravati,^{1,a)} Jan H. Los,^{2,b)} Thomas D. Kühne,^{2,c)} and Marco Bernasconi^{1,d)}

¹*Dipartimento di Scienza dei Materiali, Università di Milano-Bicocca, Via R. Cozzi 55, I-20125 Milano, Italy*

²*Institute of Physical Chemistry and Center for Computational Sciences, Johannes Gutenberg University Mainz, Staudinger Weg 7, D-55128 Mainz, Germany*

(Received 4 March 2016; accepted 3 May 2016; published online 27 May 2016)

We have investigated the structural, vibrational, and electronic properties of the amorphous phase of InSb and In₃SbTe₂ compounds of interest for applications in phase change non-volatile memories. Models of the amorphous phase have been generated by quenching from the melt by molecular dynamics simulations based on density functional theory. In particular, we have studied the dependence of the structural properties on the choice of the exchange-correlation functional. It turns out that the use of the Becke-Lee-Yang-Parr functional provides models with a much larger fraction of In atoms in a tetrahedral bonding geometry with respect to previous results obtained with the most commonly used Perdew-Becke-Ernzerhof functional. This outcome is at odd with the properties of Ge₂Sb₂Te₅ phase change compound for which the two exchange-correlation functionals yield very similar results on the structure of the amorphous phase. *Published by AIP Publishing.* [<http://dx.doi.org/10.1063/1.4950817>]

I. INTRODUCTION

Phase change chalcogenide alloys are the active materials in optical data storage (digital versatile disk, DVD)^{1–3} and more recently they are attracting an increasing interest for several electronic applications, ranging from storage class non-volatile memories^{4–6} to neuromorphic computing.⁷ These applications exploit the fast and reversible transformation between the amorphous and crystalline phases upon heating. In the electronic non-volatile memory (phase change memories, PCMs) the two states of the memory can be discriminated, thanks to a large change in the electrical resistivity across the phase change. Although Ge₂Sb₂Te₅ (GST) is presently the material of choice for electronic applications, the search of new alloys with better functional properties is a very active area of research. To make PCMs suitable for applications in automotive technologies, for instance, the stability of the amorphous phase against recrystallization must be extended above 125 °C, but still preserving a fast phase switching.⁵

The InSbTe (IST) ternary system is currently investigated as a phase change material because of the presence of compositions with high melting⁸ and crystallization temperatures.⁹ The In₃SbTe₂ composition along the pseudobinary InSb–InTe tie line, in particular, was shown to undergo a sequence of transformations from the amorphous to the crystal through several intermediate phases with different resistivities^{10–12} that might be exploited for multibits PCMs.^{13,14}

In a previous work¹⁵ we studied the structural properties of the amorphous phase of the In₃SbTe₂ compound by means of molecular dynamics simulation based on Density Functional Theory (DFT).¹⁶ The resulting amorphous phase featured a competition between octahedral-like bonding geometries typical of the rocksalt crystalline phase of In₃SbTe₂ and tetrahedral-like geometries similar to those present in the crystalline phase of the two binary compounds InTe and InSb, which is what the ternary system can be thought to be made of.¹⁵ These different bonding configurations are closely competing¹⁵ as occurs for the octahedral- and tetrahedral-like configurations of Ge atoms in DFT models of amorphous GeSbTe alloys^{17–19} and of In in amorphous InGeTe₂.²⁰ In all the previous DFT studies mentioned above, some variants of the most popular Perdew-Burke-Ernzerhof (PBE)²¹ exchange and correlation functional were used. It has been argued, however, whether different choices of the exchange-correlation (xc) functional might sizably change the tetrahedra to octahedra ratio. For instance, the addition of the semi-empirical van der Waals correction according to Grimme²² was shown to provide a better agreement with experiments on the structure of liquid and amorphous Ge₁₅Te₈₅ which feature long and weakly interacting Te–Te chains.²³ Although this semi-empirical van der Waals correction has a marginal effect on the structure of the alloy with the GeTe composition in which Te–Te chains are absent, the more complex van der Waals density functional proposed by Lee *et al.*²⁴ (denoted as vdW-DF2) was shown to better reproduce the bond length of GeTe as well, giving rise to a more defined first coordination shell²⁵ with respect to the models generated with PBE or other semi-local functionals. Still, the vdW-DF2 functional does not change sizably the ratio between tetrahedra and octahedra in amorphous GeTe.²⁵ On the other hand the

^{a)}Present address: University of Zurich, Department of Chemistry, Winterthurerstrasse 190, CH-8057 Zurich, Switzerland.

^{b)}Radboud University, Institute for Molecules and Materials, Heyendaalseweg 135, 6525AJ Nijmegen, The Netherlands.

^{c)}Dynamics of Condensed Matter, University of Paderborn, Warburger Strasse 100, D-33098 Paderborn, Germany.

^{d)}marco.bernasconi@mater.unimib.it

Becke-Lee-Yang-Parr (BLYP)²⁶ functional has been shown to better reproduce the structural properties of liquid and amorphous GeSe₂ and GeSe compounds with respect to the PBE functional.^{27,28} In particular, the stronger electron localization of the BLYP functional leads to models of liquid GeSe with a larger fraction of tetrahedra with respect to models generated with the PBE functional.²⁸ These results on selenides raise the question on whether a similar difference in the tetrahedra to octahedra ratio between PBE and BLYP models might arise for phase change tellurides as well. Concerning GeSbTe alloys, it was shown that the PBE and BLYP functionals yield very similar structural properties for amorphous Ge₂Sb₂Te₅,²⁹ although previous simulations with smaller simulation cells³⁰ suggested a slightly larger concentration of tetrahedra with the use of the BLYP functional.

In this paper, we investigate the influence of the exchange and correlation functional on the structure of amorphous In₃SbTe₂ by comparing models generated by quenching from the melt with the BLYP functional with those generated with the PBE functional and discussed in our previous work.¹⁵ For the sake of completeness we have also revisited with the use of the BLYP functional the structural properties of the amorphous phase of the binary InSb compound that we have simulated with the PBE functional in our previous works.^{31,32} As opposed to what occurs in GeSbTe alloys, it turns out that in the case of InSb the use of the BLYP functional brings the theoretical results in better agreement with experiment by favoring the tetrahedral-like environment with respect to the octahedral-like ones. A similarly larger fraction of tetrahedral configurations is also found in the BLYP models of the ternary InSbTe alloys with respect to those generated with the PBE functional.

II. COMPUTATIONAL METHODS

The amorphous models were generated by quenching from the melt within DFT-based molecular dynamics simulations by using the scheme of Kühne *et al.*³³ In the spirit of the Car-Parrinello (CP)³⁴ approach the wavefunctions are not self-consistently optimized during the dynamics. However, in contrast to CP, large integration time steps can be used in the simulation. This scheme leads to a slightly dissipative dynamics of the type $-\gamma_D \dot{\mathbf{R}}_I$, where \mathbf{R}_I are the ionic coordinates. In Refs. 33 and 35 it is shown how to compensate for this dissipation by a modified Langevin equation in order to obtain a correct canonical sampling. This scheme is implemented in the CP2K suite of programs.^{36,37} We used the BLYP exchange-correlation functional and Goedecker-type pseudopotentials³⁸ with three, five, and six valence electrons for In, Sb, and Te, respectively. The Kohn-Sham (KS) orbitals were expanded in a Triple-Zeta-Valence plus Polarization (TZVP) Gaussian-type basis set, while the charge density has been expanded in a planewave basis set with a cut-off of 100 Ry to efficiently solve the Poisson equation within periodic boundary conditions using the Quickstep scheme.^{36,37} Brillouin zone integration was restricted to the supercell Γ -point. An integration time step of 2 fs was used. Temperature was enforced by the Langevin thermostat mentioned above.

The InSb compound was modeled by a cubic supercell with 216 atoms at the density of the crystalline phase of 0.0295 atoms/Å³ (5.775 g/cm³) as in previous simulations with the PBE functional³¹ and in molecular dynamics simulations with a classical interatomic potential.³⁹ The liquid model was first equilibrated at 1000 K and then quenched to 300 K in 100 ps. We remark that the equilibrium lattice parameter and bulk modulus of crystalline InSb in the zincblende geometry are 6.575 Å and 35 GPa with the BLYP functional and 6.622 Å and 35 GPa with the PBE functional, to be compared with the experimental values of 6.479 Å and 46.5 GPa.⁴⁰

In our previous work,¹⁵ we generated models of a-In₃SbTe₂ by quenching from the melt at two fixed densities with the PBE functional. In the lack of experimental information on the density we initially fixed the density of the liquid to the value 6.448 g/cm³ (0.0323 atoms/Å³) which is about 7% lower than the density of 6.96 g/cm³ that can be assigned to the ideal rocksalt crystal with the experimental lattice parameter of 6.126(1) Å.^{41,42} A similar increase in density upon crystallization of the amorphous is found in phase change GeSbTe alloys.² An amorphous model was then generated by quenching the liquid at fixed density from 1000 K to 300 K in about 250 ps. The theoretical equilibrium density of the amorphous model was then obtained from a Murnaghan fitting of the energy-volume data of the optimized geometries at zero temperature. The resulting theoretical equilibrium density is 5.75 g/cm³ (0.0288 atoms/Å³) which is about 11% lower than our starting density of the liquid. A second amorphous model was then generated by quenching from the melt in about 350 ps at the fixed density of 5.75 g/cm³.

To investigate the effect of a different choice of the xc functional, in this work the In₃SbTe₂ compound was modeled by a cubic supercell with 300 atoms at the same density of 5.75 g/cm³ (0.0288 atoms/Å³) or 6.448 g/cm³ (0.0323 atoms/Å³) of the models generated previously with the PBE functional.¹⁵ The liquid was first equilibrated at 1000 K and then an amorphous model was obtained by quenching to 300 K in 100 ps.

We also performed constant pressure simulations during the quenching by using the Inverse Simulated Annealing (ISA) method introduced recently.^{32,43} The ISA method is a Monte Carlo (MC) annealing scheme, designed to combine the accuracy of *ab initio* calculations with the reverse MC technique^{44,45} in order to efficiently generate low energy structures in best agreement with available experimental data. Here we will use ISA merely as a minimization tool, i.e., without any experimental constraints. As such, ISA has been shown to be quite competitive in the application to amorphous phases with respect the more standard annealing procedure using molecular dynamics in the sense that it yields very similar structures but in significantly less computation time.⁴³ The hybrid MC-based ISA method introduced in our previous works^{32,43} is a “fuzzy” hybrid MC method with all atom trial moves generated by a single, energy conserving, velocity-Verlet MD step but with a randomly chosen time step $dt \in (0, dt_{max})$, where dt_{max} is adjusted on-the-fly to achieve an acceptance of 50%. To perform isobaric simulations, also volume moves are allowed with an acceptance probability

equal to that in standard MC simulation within the NPT ensemble. Typically, dt_{max} turns out to be much larger (up to an order of magnitude) than in a normal MD simulation. Further details can be found in Ref. 32.

In constant pressure simulations as well as in constant volume simulations of In_3SbTe_2 , we also added van der Waals (vdW) corrections according to Grimme²² to better reproduce the equilibrium density. The constant pressure ISA simulations provided a model of $\alpha\text{-In}_3\text{SbTe}_2$ at zero pressure at an equilibrium density of 5.554 g/cm^3 ($0.0278 \text{ atoms/\AA}^3$). The structural properties of the BLYP models at the two densities of 5.75 g/cm^3 and 5.554 g/cm^3 are, however, very similar as discussed in Sec. III B.

III. RESULTS

A. InSb

In our previous work³¹ we generated models of $\alpha\text{-InSb}$ by quenching from the liquid phase within DFT-MD simulation using the PBE functional.

It was found that short quenches (50 ps–130 ps from the melting point to 300 K) with an accurate double-zeta-valence plus polarization (DZVP) basis set give rise to a large fraction of octahedral-like local geometries and pair correlation functions (PCFs) in strong disagreement with experiments. Instead, a quench 350 ps long with a more contracted basis set leads to a model lower in energy (once optimized with the accurate DZVP basis set), with mostly tetrahedral local geometries and in good agreement with the experimental pair correlation function inferred from x-ray data.⁴⁶ However, it later turned out that the mostly tetrahedral model of Ref. 32 was actually resulting from the use of the too contracted basis set rather than from the long quenching time of 350 ps.³² In fact, simulations with similarly long quenches and the accurate DZVP basis set invariably lead to models with a large fraction of octahedral-like local geometries, in one case also lower in energy than the mostly tetrahedral-like model. We remark that the accurate DVZP and the TZVP basis sets used here have been extensively validated against calculations with a plane wave basis sets and the same pseudopotentials which actually revealed that the more contracted basis set used only in the quenching protocol employed in Ref. 31 was not sufficiently accurate.

The octahedral-like geometries have bonding angles at about 90° and 180° but coordination lower than six, actually four or five. These structures have been referred to as defective octahedra in previous DFT works on InSbTe alloys¹⁵ and other amorphous tellurides.^{17–20,47–54} Three-fold coordination with bonding angles of 90° corresponds instead to a pyramidal geometry which is also found for Sb. Snapshots of tetrahedral, defective-octahedral and pyramidal geometries are shown in Fig. 1. Actually, it is known experimentally that $\alpha\text{-InSb}$ crystallizes in a cubic rocksalt phase under moderate pressure of 1–1.3 GPa⁵⁵ which would correspond to a density increase of only 4% by assuming a crystalline-like bulk modulus of 35 GPa.³¹ It is therefore conceivable that a close competition arises between octahedral-like and tetrahedral-like local geometries. In Ref. 32 we reported on the energetics and structure of different models of $\alpha\text{-InSb}$ generated in

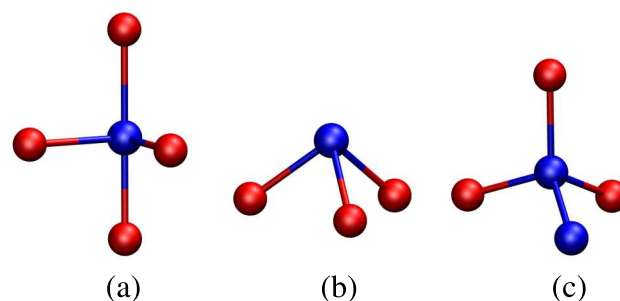


FIG. 1. Snapshot of Sb atoms in (a) defective octahedra, (b) pyramids, and (c) tetrahedra. Sb atoms are depicted by blue spheres, while In atoms by red spheres.

different manners with the PBE functional. The lowest energy model (MD-2) obtained with the accurate DZVP basis set and a long quench (350 ps) features a mostly defective-octahedral local geometry. However, the model discussed in Ref. 31, and generated with the more contracted basis set, is mostly tetrahedral and in good agreement with experiments, although it is higher in energy than the model MD-2.³² It actually turns out that the model generated with the BLYP functional is also mostly tetrahedral and very similar to the PBE model reported in Ref. 31. The total pair correlation function of the $\alpha\text{-InSb}$ models generated with BLYP and PBE (lowest energy MD-2 model, cf., Ref. 32) at the same density of 5.775 g/cm^3 is compared with the experimental x-ray data from Ref. 46 in Fig. 2. The BLYP model much better reproduces the experimental data than the lowest energy PBE (MD-2) model generated with the accurate basis set.

Information on the differences in the structural properties between the two models (BLYP and PBE MD-2) is gained from the comparison of the partial PCFs (Fig. 3), the average partial coordination numbers (Table I), the fraction of the different types of bonds (Table I), the distribution of the coordination numbers (Fig. 4), and the bond angle distribution function (Fig. 5). The partial PCFs of the BLYP model display a more compact first coordination shell with well defined minima that allow an unambiguous definition of the bonding cutoff for the calculation of the coordination numbers. On the contrary, the coordination shells of the PBE model look very

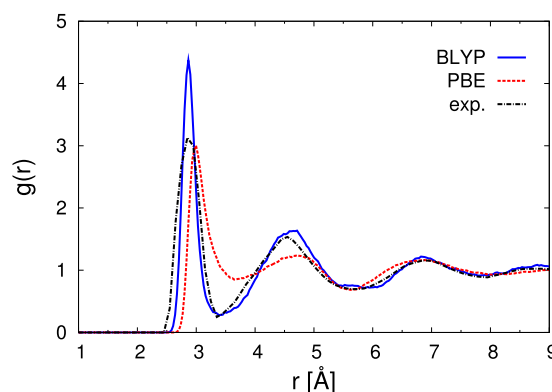


FIG. 2. Total pair correlation function of $\alpha\text{-InSb}$ at the density of 5.775 g/cm^3 computed with the BLYP (continuous line) and the PBE functional (dashed line) compared with the experimental x-ray data from Ref. 46 (dotted-dashed line).

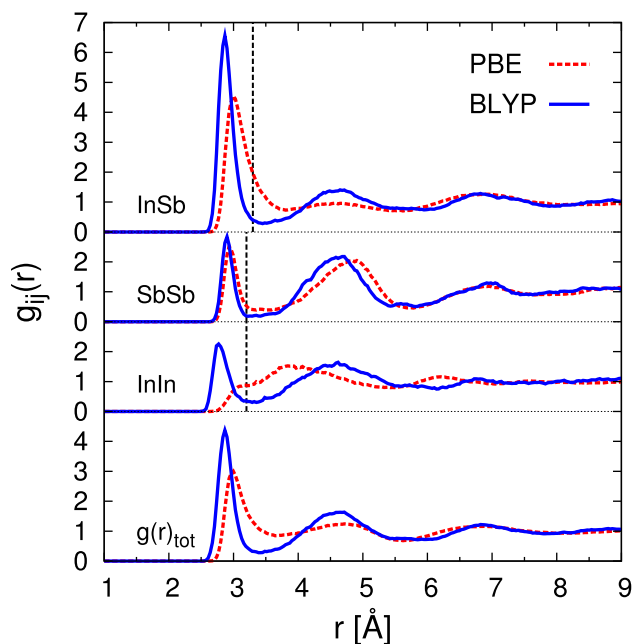


FIG. 3. Total and partial pair correlation functions of a-InSb at the density of 5.775 g/cm³ computed with the BLYP functional (continuous line) and the PBE functional (dashed line). The vertical lines are the bonding cutoff used to define the coordination numbers, namely, 3.20 Å, 3.30 Å, and 3.20 Å, for the In-In, In-Sb, and Sb-Sb bonds, respectively, in the BLYP model and (not shown) 3.30 Å, 3.50 Å, and 3.25 Å, for the In-In, In-Sb, and Sb-Sb bonds, respectively in the PBE model.

broad with a first minimum at an anomalously high distance which cannot correspond to really bonded atoms. In the PBE model the choice of the bonding cutoff cannot be reliably assigned on the basis of the bonding geometry only, but it would require the analysis of the electronic structure as well. We have not performed such an analysis here because it does not seem to be so critical in the case of the BLYP models we are interested in. The choice of the bonding cutoff for the PBE model is therefore subject to an arbitrariness which, however, does not affect the overall conclusions drawn below on the comparison between the PBE and BLYP results.

The coordination numbers are larger in the PBE model than in the BLYP models, in particular due to the presence of several 5-fold coordinated Sb atoms (cf., Fig. 4). The distribution of bond angles for Sb is also strikingly different in the BLYP and PBE models due to a different ratio of tetrahedral and defective octahedral configurations. Apparently the PBE functional strongly favors the defective

TABLE I. Average coordination numbers for different pairs of atoms computed from the partial pair correlation functions (cf., Fig. 3) of the BLYP model of a-InSb at 5.775 g/cm³. The percentage of the different types of bonds with respect to the total number of bonds is also given. Data for the model generated with the PBE functional at the same density are reported in parenthesis.

	Average coordination numbers			Types of bonds (%)	
	With In	With Sb	Total	With In	With Sb
In	1.0 (0.6)	2.9 (3.4)	3.9 (4.0)	In 13 (7)	74 (80)
Sb	2.9 (3.4)	1.0 (1.1)	3.9 (4.5)	Sb	13 (13)

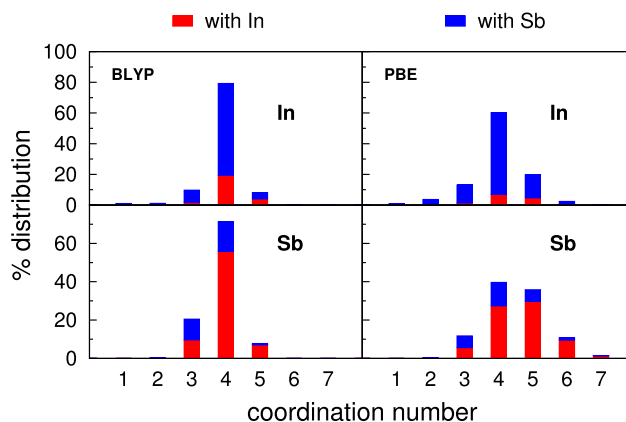


FIG. 4. Distribution of the coordination numbers of a-InSb at the density of 5.775 g/cm³ computed with the BLYP functional (left panel) and the PBE functional (right panel). The contributions from the different pairs of atoms are indicated by different colors.

octahedral configuration for Sb which also leads to a broader pair correlation function and a less defined first coordination shell.

To quantify the fraction of defective-octahedral and tetrahedral configurations we used the local order parameter q introduced in Ref. 56 as an indicator of the tetrahedrality of the bonding geometry. It is defined by $q = 1 - \frac{3}{8} \sum_{i>k} (\frac{1}{3} + \cos \theta_{ijk})^2$ where the sum runs over the pairs of atoms bonded to a central atom j and forming a bonding angle θ_{ijk} . The order parameter evaluates to $q = 1$ for the ideal tetrahedral geometry, to $q = 0$ for the six-coordinated octahedral site, and to $q = 5/8$ for a four-coordinated defective octahedral site. The distribution of the q parameter for the BLYP and PBE models is compared in Fig. 6. The concentration of atoms in tetrahedral geometry can be obtained by integrating the q distribution for 4-coordinated atoms from $q = 0.8$ to its upper limit as discussed in Refs. 15, 20, and 52, 53. We obtain a fraction of In and Sb atoms in tetrahedral geometry of 67% and 48% for the BLYP model and of 43% and 11% for the PBE (MD-2) model. The BLYP model is therefore mostly tetrahedral while the PBE model mostly features defective octahedral environments.

Concerning the medium range order, we report the distribution of ring length in Fig. 7 computed according to Ref. 57. In the PBE model the distribution of rings is rather broad, with a large abundance of 4-, 5-, and 6-membered rings. The 4-membered ring is the building block of the cubic rocksalt phase and corresponds to σ_p -bonds in defective

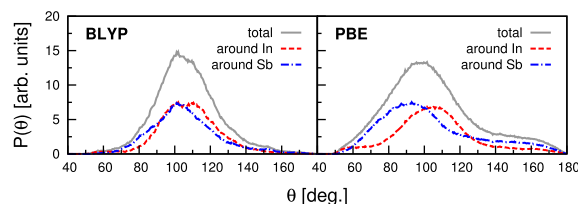


FIG. 5. Bond angles distribution of a-InSb at the density of 5.775 g/cm³ computed with the BLYP (left panel) and the PBE functional (right panel). The total distribution (continuous line) is resolved into the contributions from the bonds made by In (dashed line) and Sb (dotted-dashed line) atoms.

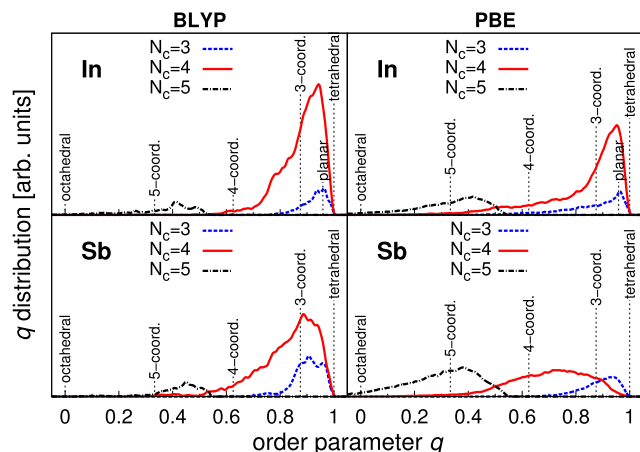


FIG. 6. Distribution of the local order parameter q for tetrahedrity (see text) for a-InSb at the density of 5.775 g/cm^3 computed with the BLYP (left panel) and the PBE functional (right panel). The distribution for In and Sb atoms are given separately in the upper and lower panels and are further resolved in the contributions from atoms with different coordination (N_c). Vertical dashed lines indicate the values of q for selected ideal defective-octahedral geometries and for the tetrahedral geometry. By integrating the q distribution from 0.8 to 1.0 we obtain a fraction of In and Sb atoms in tetrahedral geometry of 67% and 48% for the BLYP model and of 43% and 11% for the PBE model.

octahedra. It is the most abundant ring in GST and GeTe.^{17–19,50} In the BLYP model the most abundant rings are the five- and six-membered ones, typical of a mostly tetrahedral network.

Homopolar Sb–Sb bonds are arranged in clusters or chains whose distribution is reported in Fig. S1 in the supplementary material (SM).⁶⁴ A large 13-atom cluster (a branched chain), present in the model generated with the BLYP functional, is shown in Fig. S2 in the SM.

In summary, the model of a-InSb generated with the BLYP functional has a mostly tetrahedral network and reproduces well the experimental PCF. The tetrahedral bonding geometry is favored with respect to the octahedral-like geometry by the BLYP functional. In fact, once relaxed with the BLYP functional, the mostly octahedral MD-2 model generated with the PBE functional is higher in energy by about 41 meV/atom with respect to the tetrahedral-like model generated with the BLYP one. The reverse is true if we optimize with the PBE functional the tetrahedral model which becomes 29 meV/atom higher in energy than the MD-2 model at the PBE level.

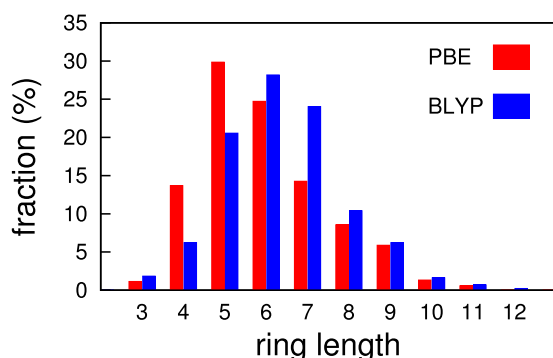


FIG. 7. Ring distribution function of a-InSb at the density of 5.775 g/cm^3 computed with the BLYP and PBE functionals.

The effect of vdW interactions on the structural properties was also investigated by generating a model of a-InSb at the same density of 5.775 g/cm^3 by quenching from the melt in 100 ps with BLYP simulations and by including vdW interactions according to Grimme.²² The only difference with respect to the BLYP model without vdW correction is a fraction of tetrahedra about 2% lower for In atoms and 2% higher for Sb atoms which are, however, within the uncertainties due to the small simulation cell.

We remark that these two models are generated at the same fixed density. The vdW corrections according to Grimme have thus a negligible effect on the short range structure at fixed volume, but they do affect the equilibrium volume. The theoretical equilibrium density of the zincblende crystal increases by about 6% with respect to BLYP calculations without vdW correction. To investigate the effect of the density on the structure of a-InSb we generated another amorphous model at the fixed density of 5.355 g/cm^3 which differs by about 8% with respect to the 5.775 g/cm^3 density of the models discussed above which in turn is slightly higher than the experimental density of 5.66 g/cm^3 of the as-deposited samples.⁴⁶ The partial coordination numbers of this second model are equal to those given in Table I within the figures given there. Therefore we can conclude that vdW corrections have an overall negligible effect on the short range topology of a-InSb.

These new results on InSb point to a deficiency of the PBE exchange-correlation functional when dealing with the close competition in energy between tetrahedral-like and octahedral-like configurations, which is probably also responsible for the tetrahedral-to-octahedral transition observed experimentally in a-InSb under moderate pressure.⁵⁵

B. In_3SbTe_2

The crystalline cubic phase of In_3SbTe_2 is thermodynamically stable only in the temperature range 470°C – 570°C , but it can be recovered upon quenching at normal conditions, bypassing the decomposition into InTe and InSb expected below 470°C . The crystal structure of cubic In_3SbTe_2 was assigned to the $\text{Fm}\bar{3}\text{m}$ space group with a lattice constant of $6.126(1) \text{ \AA}$ and a rocksalt geometry⁴¹ with In occupying the cation sublattice and Sb and Te atoms occupying the anion sublattice in a random manner as shown by recent x-ray and neutron diffraction experiments.⁴² The crystal is metallic with a conductivity of $3.2 \cdot 10^4 \text{ S/cm}$ at normal conditions.⁴²

In our previous work¹⁵ we reported a theoretical equilibrium density about 10% lower than in experiments as computed from the equation of state of the cubic crystal in a 216-atom supercell with the PBE functional. In this calculation the Brillouin zone integration was restricted to the Γ -point only which, however, turns out to be insufficient given the metallic nature of the compound. In fact, the theoretical cubic lattice parameter turns out to be 6.05 \AA , in good agreement with experiments, once the system is modeled in a hexagonal cell with six planes stacked along the c axis as In–Sb–In–Te–In–Te and six atoms per unit cell and the Brillouin zone is integrated over a $8 \times 8 \times 4$ uniform mesh⁵⁸ by using the Quantum-espresso suite of programs.⁵⁹ The

hexagonal cell was optimized by fixing the c/a ratio to the value ($2\sqrt{6}$) expected for a cubic-like symmetry. A similar hexagonal setup was used in a recent DFT work on the chemical bonding in In_3SbTe_2 .⁶⁰

The octahedral-like bonding geometry of the cubic In_3SbTe_2 crystal has to be contrasted with the tetrahedral bonding geometry of the binary compounds InTe ⁶¹ and InSb . In fact, InSb crystallizes in a zinc-blende structure, while crystalline InTe is made of chains of edge-sharing InTe_4 tetrahedra intercalated by weakly bound, interstitial-like In ions.⁶¹

In Ref. 15 we have shown that the models of the amorphous phase of In_3SbTe_2 generated with the PBE functional feature both the octahedral (defective) local geometry similar to those present in the ternary cubic crystal and the tetrahedral geometries present in the two parent binary compounds. The abundance of the different bonding geometries in the amorphous phase was, however, strongly dependent on the density in the range 6.448–5.75 g/cm^3 that we investigated. At high density the bonding topology was mostly octahedral-like (18% of tetrahedral In atoms) while at low density a fraction as large as 41% of In atoms had a tetrahedral-like bonding geometry.

The models of $\text{a-In}_3\text{SbTe}_2$ generated here with the BLYP functional at the same two densities of 6.448 g/cm^3 (0.0323 atoms/ \AA^3) and 5.75 g/cm^3 (0.0288 atoms/ \AA^3) investigated previously (cf., Sec. II) show a much more pronounced tetrahedral character with respect to the PBE models. In fact, 63% and 70% of In atoms are in a tetrahedral geometry at high and low densities. A similar fraction of 66% of In atoms are in a tetrahedral geometry at the equilibrium density of 5.554 g/cm^3 (0.0278 atoms/ \AA^3) obtained from the constant pressure ISA simulations. The dependence of the structural properties on the density is thus much less striking with the BLYP functional than with the PBE functional.

Information on the differences in the structural properties between the models generated with the two functionals at the

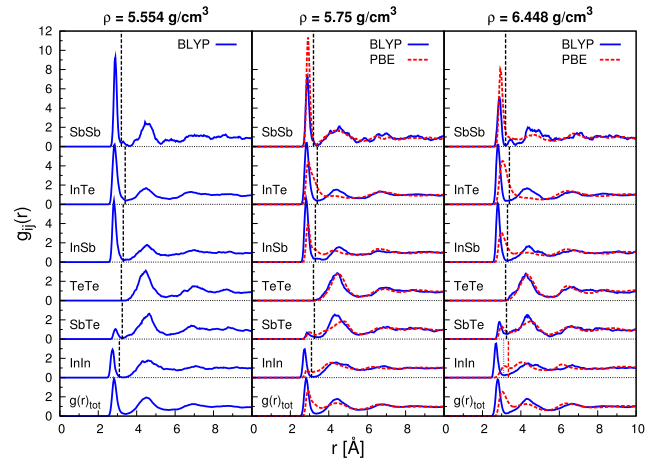


FIG. 8. Total and partial pair correlation functions of $\text{a-In}_3\text{SbTe}_2$ models generated with the BLYP (continuous lines) and PBE (dashed lines) functionals at the density of 5.554 g/cm^3 (left panel), 5.75 g/cm^3 (central panel), or 6.448 g/cm^3 (right panel). The vertical lines are the bonding cutoff used to define the coordination numbers (3.10 or 3.35 \AA , 3.30 \AA , 3.40 \AA , 3.25 \AA , 3.20 \AA , and 3.20 \AA , for the In-In , In-Sb , In-Te , Sb-Te , Sb-Sb , and Te-Te bonds, respectively).

TABLE II. Average coordination numbers for different pairs of atoms computed from the partial pair correlation functions (cf., Fig. 8) for $\text{a-In}_3\text{SbTe}_2$ models generated with the BLYP functional and the PBE functional (in parenthesis) at the density of 5.75 g/cm^3 (upper table), 6.448 g/cm^3 (central table), and 5.554 g/cm^3 (lower table).

	With In	With Sb	With Te	Total
In	0.9 (0.4)	0.9 (0.7)	2.0 (2.3)	3.8 (3.3)
Sb	2.6 (2.0)	0.8 (1.3)	0.2 (0.3)	3.7 (3.6)
Te	3.0 (3.4)	0.1 (0.2)	0.0 (0.0)	3.1 (3.6)
	With In	With Sb	With Te	Total
In	1.3 (1.0)	0.9 (0.8)	2.0 (2.7)	4.1 (4.5)
Sb	2.6 (2.4)	0.7 (1.2)	0.6 (0.6)	3.9 (4.2)
Te	3.0 (4.0)	0.3 (0.3)	0.0 (0.0)	3.3 (4.3)
	With In	With Sb	With Te	Total
In	1.0	0.8	1.9	3.7
Sb	2.4	0.9	0.3	3.6
Te	2.9	0.1	0.0	3.0

two densities is gained from the comparison of the partial PCFs (Fig. 8), the average partial coordination numbers (Table II), the fraction of the different types of bonds (Table III), the distribution of the coordination numbers (Fig. 9), the bond angle distribution function (Fig. 10), and the distribution of the local order parameter q for tetrahedrality (Fig. 11). The corresponding data for the BLYP model at the equilibrium density of 5.554 g/cm^3 obtained from constant pressure ISA simulations (cf., Sec. II) are also given for the sake of comparison.

The same caveats on the choice of the bonding cutoff for the PBE models discussed in Section III A for InSb hold here for the ternary alloy. In the BLYP models the first peak of the pair correlation function is higher and sharper, the coordination numbers are lower at all densities, and their distribution better peaked around four for In/Sb and three for Te than in the PBE models. In the BLYP models there is also a slightly larger fraction of In-Sb and In-In bonds than in the

TABLE III. Percentage of the different types of bonds with respect to the total number of bonds for models of $\text{a-In}_3\text{SbTe}_2$ generated with the BLYP functional and the PBE functional (in parenthesis) at the density of 5.75 g/cm^3 (upper table), 6.448 g/cm^3 (central table), and 5.554 g/cm^3 (lower table).

	With In	With Sb	With Te
In	13 (5)	25 (20)	56 (66)
Sb		4 (6)	2 (3)
Te			0 (0)
	With In	With Sb	With Te
In	17 (12)	23 (18)	52 (62)
Sb		3 (4)	6 (4)
Te			0 (0)
	With In	With Sb	With Te
In	14	23	56
Sb		4	3
Te			0

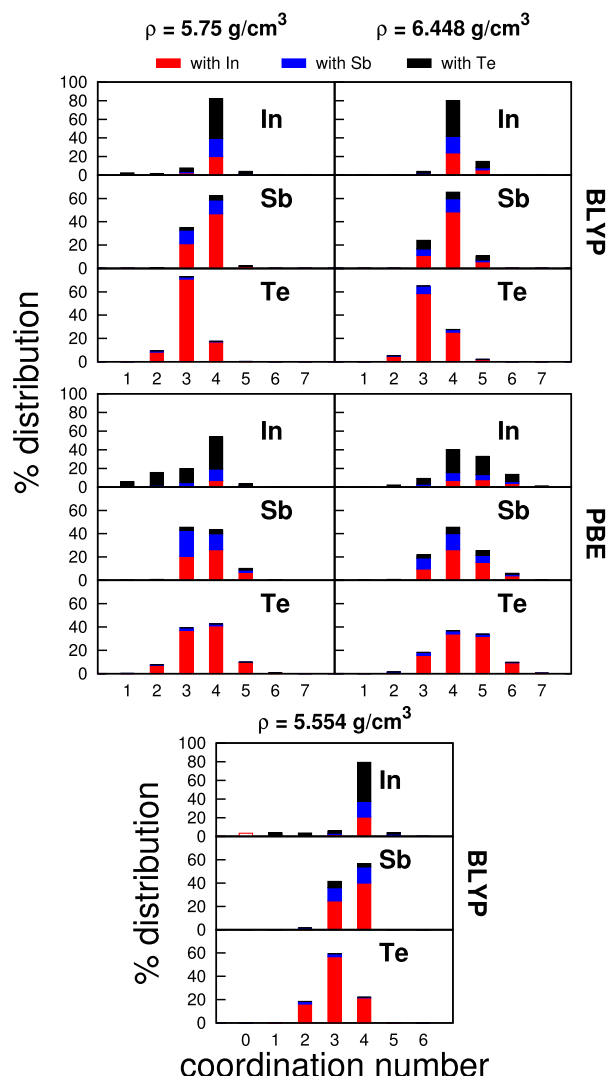


FIG. 9. Distribution of the coordination numbers of a-In₃SbTe₂ models generated with the BLYP (top panels) and PBE (central panels) functionals at the density of 5.75 g/cm³ (left panels) or 6.448 g/cm³ (right panels). The contributions from the different pairs of atoms are indicated by different colors. The data for the BLYP model at the theoretical equilibrium density of 5.554 g/cm³ are reported in the bottom panel.

PBE models. The maximum of the bond angle distribution function is clearly shifted towards larger angles in the BLYP models due to a larger fraction of tetrahedra.

Integration of the q order parameter for tetrahedrality leads to the estimates of the fraction of tetrahedral atoms as given at the beginning of the section and in the caption of Fig. 11. The distribution of the different types of tetrahedra (isolated, edge-, corner-sharing) is given in Table IV for the BLYP and PBE models. The overwhelming majority of tetrahedra is corner-sharing with a fraction of edge-sharing tetrahedra increasing with the overall fraction of tetrahedra, i.e., at lower density. The statistics of the different types of local environments are reported in Tables SI-SIII in the supplementary material for the BLYP models at the three densities.⁶⁴ The distribution of ring length is shown in Fig. 12. The 4-membered ring typical of defective-octahedral structures is sizably lower in the mostly tetrahedral BLYP models than in the PBE ones.

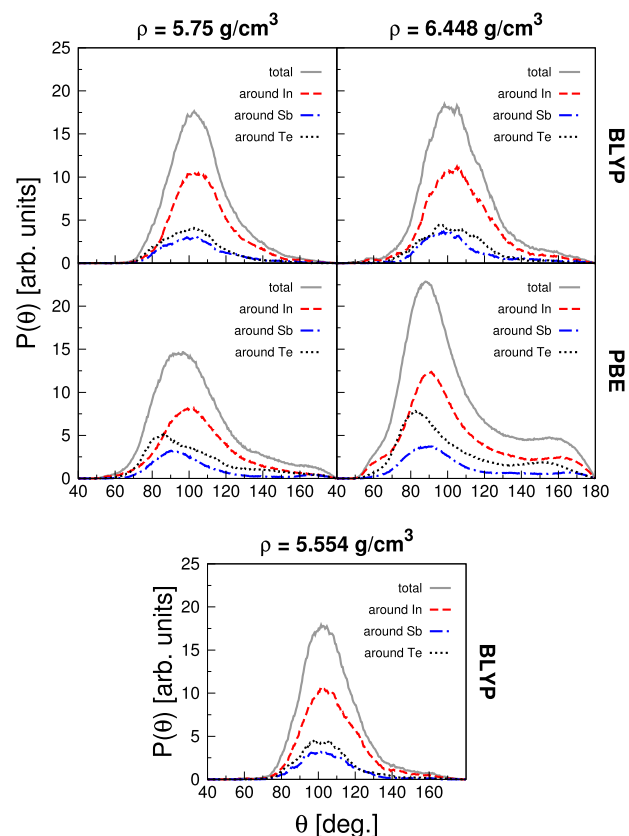


FIG. 10. Bond angles distribution of a-In₃SbTe₂ models generated with the BLYP functional (top panels) and the PBE functional (central panels) at the density of 5.75 g/cm³ (left panels) or 6.448 g/cm³ (right panels). The total distribution (continuous line) is resolved into the contributions from the bonds made by In (dashed line), Sb (dotted-dashed line), and Te (dotted line) atoms. The data for the BLYP model at the theoretical equilibrium density of 5.554 g/cm³ are reported in the bottom panel.

The distribution of the size of Sb clusters in the models of a-In₃SbTe₂ is reported in Fig. S3 in the supplementary material.⁶⁴ The number and size of Sb clusters are clearly much lower in a-In₃SbTe₂ than in a-InSb because of a lower fraction of Sb–Sb bonds in the former system clearly related to an overall lower fraction of Sb atoms.

Overall, the BLYP models have a much larger fraction of tetrahedra than the PBE models which reflects in all changes in topology of the network and in a much milder dependence of the structure on the density than previously suggested on the basis of the PBE results.¹⁵

Electronic and vibrational properties: The electronic Density of States (DOS) of the BLYP models of a-In₃SbTe₂ is shown in Fig. 13 as computed from KS orbitals at the supercell Γ -point. The band gap decreases by increasing density and, as expected, it is overall smaller than the gap computed with the hybrid functional⁶² for the PBE models in Ref. 15.

The phonon DOS was computed from the diagonalization of the dynamical matrix obtained in turn from the variation of atomic forces due to finite atomic displacements 0.0053 Å large. Only phonons with the periodicity of our supercell (Γ -point phonons) were considered. The corresponding DOS for the models generated with the PBE functionals at 6.448 g/cm³ and 5.75 g/cm³ is reported in Ref. 15 to which we refer to for the sake of comparison. In

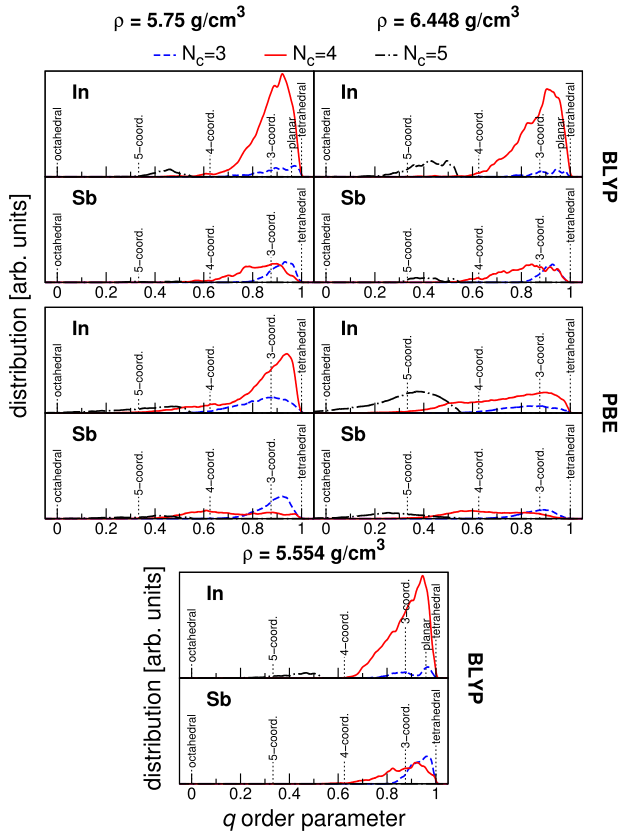


FIG. 11. Distribution of the local order parameter q for tetrahedrality (see text) of a-In₃SbTe₂ models generated with the BLYP (top panels) and PBE (central panels) functionals at the density of 5.75 g/cm³ (left panel) or 6.448 g/cm³ (right panel). The distribution for In, Sb, and Te atoms are given separately and are further resolved in the contributions from atoms with different coordination (N_c). Vertical dashed lines indicate the values of q for selected ideal defective-octahedral geometries and for the tetrahedral geometry. The data for the BLYP model at the theoretical equilibrium density of 5.554 g/cm³ are reported in the bottom panel.

Fig. 14 we also show the inverse participation ratio (IPR) that quantifies the degree of localization of each phonon. The IPR of the j th vibrational mode is defined as

$$IPR = \frac{\sum_m \left| \frac{\mathbf{e}(j,m)}{\sqrt{M_m}} \right|^4}{\left(\sum_m \frac{|\mathbf{e}(j,m)|^2}{M_m} \right)^2}, \quad (1)$$

TABLE IV. Statistics of the connectivity of tetrahedra for models a-In₃SbTe₂ generated with the BLYP and PBE functionals at the density of 5.75 g/cm³, 6.448 g/cm³, and 5.554 g/cm³. The absolute numbers of tetrahedra of the different types are given in parenthesis.

Tetrahedra statistics			
Model	Isolated	Corner-sharing	Edge-sharing
BLYP 5.554 g/cm ³	...	84% (91)	16% (17)
BLYP 5.75 g/cm ³	1% (1)	71% (82)	28% (33)
PBE 5.75 g/cm ³	1% (1)	68% (48)	31% (22)
BLYP 6.448 g/cm ³	...	94% (99)	6% (6)
PBE 6.448 g/cm ³	12% (4)	82% (28)	6% (2)

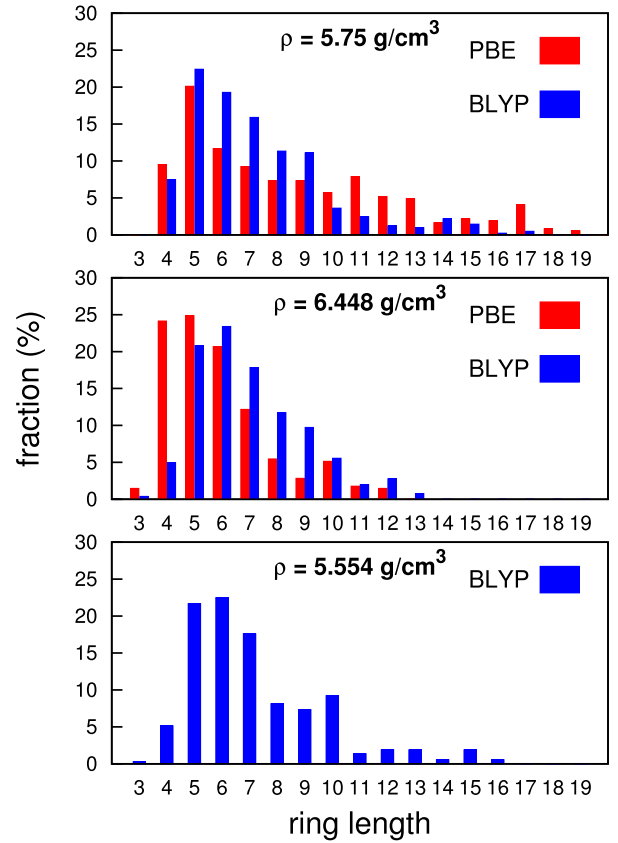


FIG. 12. Ring statistics of a-In₃SbTe₂ models generated with the BLYP and PBE functionals at the density of 5.75 g/cm³ (top panel), 6.448 g/cm³ (central panel), and 5.554 g/cm³ (bottom panel).

where $\mathbf{e}(j,m)$ are phonon eigenvectors, while the sum over m runs over the N atoms in the unit cell with masses M_m . According to this definition, the value of the IPR varies from $1/N$ for a completely delocalized phonon, to one for a mode completely localized on a single atom. Phonons above 150 cm⁻¹ are mostly localized on tetrahedra centered on In. Note that due to the increased fraction of tetrahedra, the phonon DOS extends to higher frequencies with respect to

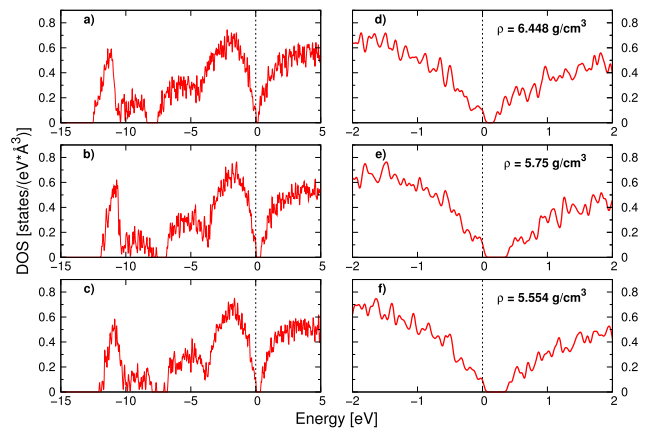


FIG. 13. Electronic density of states (BLYP functional) for the models of a-In₃SbTe₂ at density of (a) 6.448 g/cm³, (b) 5.75 g/cm³, and (c) 5.554 g/cm³. The KS energies are broadened by Gaussian functions of 27 meV width. The zero of energy corresponds to the top of the valence band. (d)-(f) A zooming of the DOS of panels (a)-(c) close to the band gap.

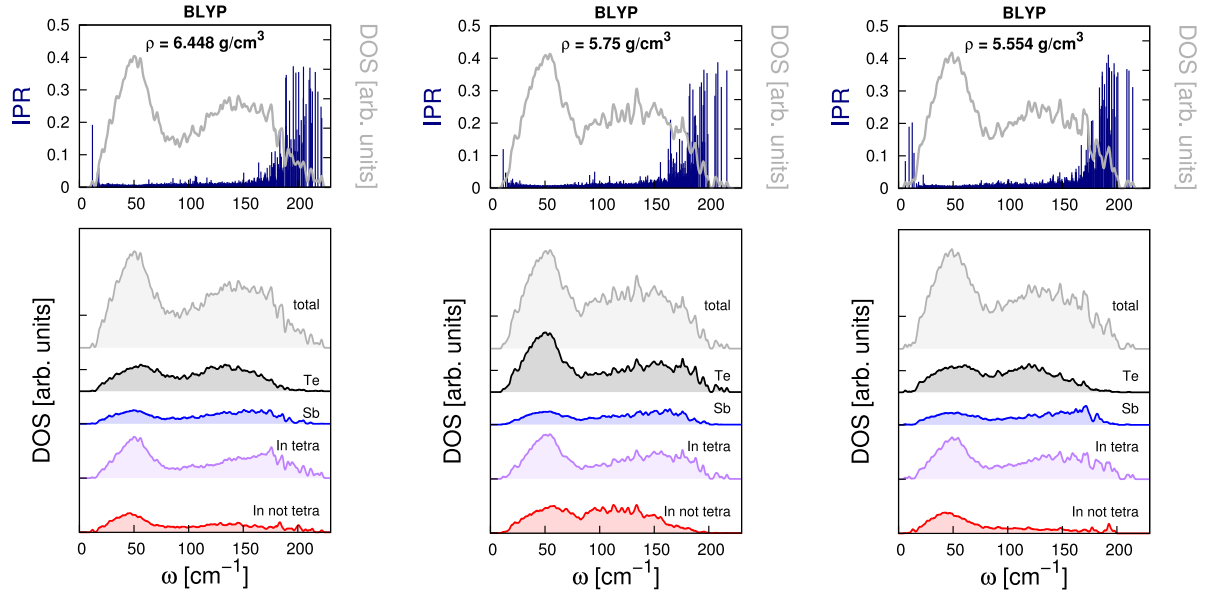


FIG. 14. Theoretical phonon DOS of the BLYP models of a-In₃Sb₁Te₂ at density of 6.448 g/cm³ (left panels), 5.75 g/cm³ (central panels), and 5.554 g/cm³ (right panels). The phonon IPR (blue spikes, see text for definition) is superimposed to the DOS in the upper panels. Projections on different species (Sb, Te, tetrahedral In, and non-tetrahedral In) are reported in the lower panels.

those of the more octahedral models generated with the PBE functional and reported in Ref. 15.

From the projected DOS we also computed the Debye-Waller factor for each species defined by⁶³

$$B_{\kappa} = \frac{8\pi^2}{3} \langle \mathbf{u}_{\kappa}^2 \rangle, \quad (2)$$

where κ runs over the three species and $\langle \mathbf{u}_{\kappa}^2 \rangle$ is the mean average square displacement of atoms of species κ computed from harmonic phonons as

$$\langle \mathbf{u}_{\kappa}^2 \rangle = \sum_{j,m} \frac{\hbar}{\omega_j} \frac{|\mathbf{e}(j,m)|^2}{M_{\kappa}} \left[n_B \left(\frac{\hbar \omega_j}{k_B T} \right) + \frac{1}{2} \right], \quad (3)$$

where m runs over atoms of species κ , and ω_j is frequency of the j th harmonic phonon. The temperature dependence is introduced by the Bose factor n_B .

The resulting Debye-Waller factors as a function of temperature are reported in Fig. 15; they are sizably lower than the values reported previously for the PBE models¹⁵ because of the overall blueshift of the phonon frequencies in the BLYP models due to higher fraction of tetrahedra.

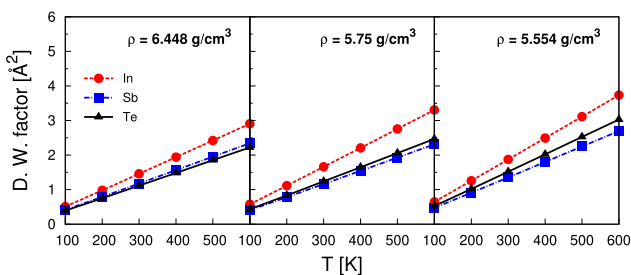


FIG. 15. Debye-Waller factor B_{κ} defined by Eq. (2) of In, Sb and Te atoms as a function of temperature in the BLYP models of a-In₃Sb₁Te₂ at the three densities.

The calculated Debye-Waller factor averaged over the three species at 300 K is about 1.67 Å² in the model at 5.554 g/cm³ which is very close to the value of 1.52 Å² measured experimentally from the Rietveld analysis of the crystalline cubic phase of In₃SbTe₂ in Ref. 42. However, we must consider that the latter experimental value includes the static displacement with respect to the ideal rocksalt geometry due to disorder. The theoretical thermal mean square displacement in the amorphous phase is therefore larger than the experimental value in the crystalline phase. The average Debye-Waller B factor at 300 K of amorphous In₃SbTe₂ is also close to the corresponding theoretical value of about 2.0 Å² obtained for Ge₂Sb₂Te₅ amorphous models in Ref. 47.

IV. CONCLUSIONS

We have investigated the dependence of the structural and vibrational properties of models of amorphous In₃SbTe₂ on the choice of the exchange and correlation functional. Models of this phase change alloy generated by quenching from the melt with the BLYP functional have been compared with models generated with the most commonly used PBE functional in Ref. 15. As a preliminary investigation we have also compared PBE and BLYP models of the amorphous phase of the binary InSb compound. In both the InSb and In₃SbTe₂ compounds, the stronger electronic localization associated to the BLYP functional leads to a much larger fraction of tetrahedral configurations with respect to the PBE models that feature instead mostly defective octahedral or pyramidal bonding geometries. This outcome is similar to what has been documented for GeSe_x alloys,^{27,28} but it is at odds with the behaviour of Ge₂Sb₂Te₅ for which very similar amorphous models have been generated with the PBE and BLYP functionals.²⁹ The a-In₃SbTe₂ alloy appears as a mixture of the binary compounds InSb and InTe with very few Sb-Te bonds as already discussed for the PBE models

in Ref. 15. The BLYP models present, however, a mostly tetrahedral network whose structural features are more weakly dependent on the density than previously proposed on the basis of the PBE results.¹⁵ The strong dependence of the fraction of In and Sb in tetrahedral configurations on the choice of the exchange and correlation functional originates from the closeness in energy of the octahedral configurations. Indeed, a-InSb is known to crystallize in the zincblende phase at normal conditions and in the rocksalt phase at a moderate pressure of 1–1.3 GPa.⁵⁵ It actually turns out that the BLYP functional favors more strongly the zincblende phase with respect to the rocksalt one in crystalline InSb, the difference between the two phases at their equilibrium density at zero temperature being about 0.548 eV/atom with the BLYP and 0.231 eV/atom with the PBE functional.

Overall, the quest for an optimal description of bonding in Te-based amorphous phase change alloys seems to deserve further investigations for instance with other functionals such as hybrid functionals⁶² or functionals with non-local van der Waals corrections.²⁴

ACKNOWLEDGMENTS

J.L. and T.D.K. would like to acknowledge financial support from the IDEE project of the Carl-Zeiss Foundation and the Graduate School of Excellence MAINZ. S.G. and M.B. acknowledge funding from the European Union Seventh Framework Programme No. FP7/2007-2013 under Grant Agreement No. 310339.

- ¹M. Wuttig and N. Yamada, *Nat. Mater.* **6**, 824 (2007).
- ²D. Lencer, M. Salinga, and M. Wuttig, *Adv. Mater.* **23**, 2030 (2011).
- ³S. Raoux, W. Welnic, and D. Ielmini, *Chem. Rev.* **110**, 240 (2010).
- ⁴A. Pirovano, A. L. Lacaita, A. Benvenuti, F. Pellizzer, and R. Bez, *IEEE Trans. Electron Devices* **51**, 452 (2004).
- ⁵A. L. Lacaita and A. Redaelli, *Microelectron. Eng.* **109**, 351 (2013).
- ⁶G. W. Burr et al., *IBM J. Res. Dev.* **22**, 449 (2008).
- ⁷C. D. Wright, Y. Liu, K. I. Kohary, M. M. Aziz, and R. J. Hicken, *Adv. Mater.* **23**, 3408 (2011); D. Kuzum, R. G. D. Jeyasingh, B. Lee, and H.-S. P. Wong, *Nano Lett.* **12**, 2179 (2012).
- ⁸H. J. Shin, Y. S. Kang, A. Benayad, K. H. Kim, Y. M. Lee, M. C. Jung, T. Y. Lee, D. S. Suh, K. H. P. Kim, C. K. Kim, and Y. Khang, *Appl. Phys. Lett.* **93**, 021905 (2008).
- ⁹Y. Maeda, H. Andoh, I. Ikuta, and H. Minemura, *J. Appl. Phys.* **64**, 1715 (1988).
- ¹⁰E. T. Kim, J. Y. Lee, and Y. T. Kim, *Phys. Status Solidi RRL* **3**, 103 (2009).
- ¹¹Y. T. Kim, E. T. Kim, C. S. Kim, and J. Y. Lee, *Phys. Status Solidi RRL* **5**, 98 (2011).
- ¹²R. Fallica, T. Stoycheva, C. Wiemer, and M. Longo, *Phys. Status Solidi RRL* **11**, 1009 (2013).
- ¹³N. Papandreou, A. Pantazi, A. Sebastian, E. Eleftheriou, M. Breitwisch, C. Lam, and H. Pozidis, *Solid-State Electron.* **54**, 991 (2010).
- ¹⁴K. Daly-Flynn and D. Strand, *Jpn. J. Appl. Phys., Part 1* **42**, 795 (2003).
- ¹⁵J. H. Los, T. D. Kühne, S. Gabardi, and M. Bernasconi, *Phys. Rev. B* **88**, 174203 (2013).
- ¹⁶R. O. Jones, *Rev. Mod. Phys.* **87**, 897 (2015).
- ¹⁷S. Caravati, M. Bernasconi, T. D. Kühne, M. Krack, and M. Parrinello, *Appl. Phys. Lett.* **91**, 171906 (2007).
- ¹⁸J. Akola and R. O. Jones, *Phys. Rev. B* **76**, 235201 (2007).
- ¹⁹J. Hegedüs and S. R. Elliott, *Nat. Mater.* **7**, 399 (2008).
- ²⁰E. Spreafico, S. Caravati, and M. Bernasconi, *Phys. Rev. B* **83**, 144205 (2011).
- ²¹J. P. Perdew, K. Burke, and M. Ernzerhof, *Phys. Rev. Lett.* **77**, 3865 (1996).
- ²²S. Grimme, J. Antony, S. Ehrlich, and H. Krieg, *J. Chem. Phys.* **132**, 154104 (2010).
- ²³M. Micoulaut, *J. Chem. Phys.* **133**, 061103 (2013); M. Micoulaut, M.-V. Coulet, A. Piarristeguy, M. Johnson, C. J. Cuello, C. Bichara, H. Flores-Ruiz, and Pradel A., *Phys. Rev. B* **89**, 174205 (2014); M. Micoulaut, K. Gunasekera, S. Ravindren, and P. Boolchand, *ibid.* **90**, 094207 (2014).
- ²⁴K. Lee, E. D. Murray, L. Kong, B. I. Lundqvist, and D. C. Langreth, *Phys. Rev. B* **82**, 081101 (2010).
- ²⁵J. Y. Raty, W. Zhang, J. Luckas, C. Chen, R. Mazzarello, C. Bichara, and M. Wuttig, *Nat. Commun.* **7**, 7467 (2015).
- ²⁶A. D. Becke, *Phys. Rev. A* **38**, 3098 (1988); C. Lee, W. Yang, and R. G. Parr, *Phys. Rev. B* **37**, 785 (1988).
- ²⁷M. Micoulaut, R. Vuilleumier, and C. Massobrio, *Phys. Rev. B* **79**, 214205 (2009).
- ²⁸S. Le Roux, A. Bouzid, M. Boero, and C. Massobrio, *J. Chem. Phys.* **138**, 174505 (2013).
- ²⁹S. Caravati and M. Bernasconi, *Phys. Status Solidi B* **252**, 261 (2015).
- ³⁰K. Y. Kim, D.-Y. Cho, B.-Ki Cheong, D. Kim, H. Horii, and S. Han, *J. Appl. Phys.* **113**, 134302 (2013).
- ³¹J. H. Los, T. D. Kühne, S. Gabardi, and M. Bernasconi, *Phys. Rev. B* **87**, 184201 (2013).
- ³²J. H. Los, S. Gabardi, M. Bernasconi, and T. D. Kühne, *Comput. Mater. Sci.* **117**, 7 (2016).
- ³³T. D. Kühne, M. Krack, F. R. Mohamed, and M. Parrinello, *Phys. Rev. Lett.* **98**, 066401 (2007).
- ³⁴R. Car and M. Parrinello, *Phys. Rev. Lett.* **55**, 2471 (1985).
- ³⁵T. D. Kühne, M. Krack, and M. Parrinello, *J. Chem. Theory Comput.* **5**, 235 (2009).
- ³⁶J. VandeVondele, M. Krack, F. Mohamed, M. Parrinello, T. Chassaing, and J. Hutter, *Comput. Phys. Commun.* **167**, 103 (2005).
- ³⁷M. Krack and M. Parrinello, in *High Performance Computing in Chemistry NIC*, edited by J. Grotendorst (FZ Jülich, 2004), Vol. 25, pp. 29–51; www.cp2k.org.
- ³⁸S. Gödecke, M. Teter, and J. Hutter, *Phys. Rev. B* **54**, 1703 (1996); M. Krack, *Theor. Chem. Acc.* **114**, 145 (2005).
- ³⁹J. P. Rino, D. S. Borges, and S. C. Costa, *J. Non-Cryst. Solids* **348**, 17 (2004).
- ⁴⁰O. Madelung, *Semiconductors: Data Handbook* (Springer Verlag, Berlin, 2004), pp. 154–161.
- ⁴¹K. Deneke and A. Rabenau, *Z. Anorg. Allg. Chem.* **333**, 201 (1964).
- ⁴²T. Schröder, T. Rosenthal, S. Grott, C. Stiewe, J. de Boor, and O. Oeckler, *Z. Anorg. Allg. Chem.* **639**, 2536 (2013).
- ⁴³J. H. Los and T. D. Kühne, *Phys. Rev. B* **87**, 214202 (2013).
- ⁴⁴R. L. McGreevy and L. Pusztai, *Mol. Simul.* **1**, 359 (1988).
- ⁴⁵R. L. McGreevy, *J. Phys.: Condens. Matter* **13**, R877 (2001).
- ⁴⁶N. J. Shevchik and W. Paul, *J. Non-Cryst. Solids* **16**, 55 (1974).
- ⁴⁷S. Caravati, M. Bernasconi, T. D. Kühne, M. Krack, and M. Parrinello, *J. Phys.: Condens. Matter* **21**, 255501 (2009); errata, **21**, 499803 (2009); errata, **22**, 399801 (2010).
- ⁴⁸S. Caravati, M. Bernasconi, and M. Parrinello, *J. Phys.: Condens. Matter* **22**, 315801 (2010).
- ⁴⁹S. Gabardi, S. Caravati, M. Bernasconi, and M. Parrinello, *J. Phys.: Condens. Matter* **24**, 385803 (2012).
- ⁵⁰R. Mazzarello, S. Caravati, S. Angioletti-Uberti, M. Bernasconi, and M. Parrinello, *Phys. Rev. Lett.* **104**, 085503 (2010); **107**, 039902(E) (2011).
- ⁵¹A. Bouzid and C. Massobrio, *J. Chem. Phys.* **137**, 046101 (2012).
- ⁵²S. Caravati, D. Colleoni, R. Mazzarello, T. D. Kühne, M. Krack, M. Bernasconi, and M. Parrinello, *J. Phys.: Condens. Matter* **23**, 265801 (2011).
- ⁵³G. C. Sossio, S. Caravati, R. Mazzarello, and M. Bernasconi, *Phys. Rev. B* **83**, 134201 (2011).
- ⁵⁴S. Caravati, M. Bernasconi, and M. Parrinello, *Phys. Rev. B* **81**, 014201 (2010).
- ⁵⁵O. Shimomurka, A. Saumin, N. Sakai, and S. Minomura, *Philos. Mag.* **34**, 839 (1976).
- ⁵⁶J. R. Errington and P. G. Debenedetti, *Nature* **409**, 318 (2001).
- ⁵⁷D. S. Franzblau, *Phys. Rev. B* **44**, 4925 (1991).
- ⁵⁸H. J. Monkhorst and J. D. Pack, *Phys. Rev. B* **13**, 5188 (1976).
- ⁵⁹P. Giannozzi et al., *J. Phys.: Condens. Matter* **21**, 395502 (2009), <http://www.quantum-espresso.org>.
- ⁶⁰V. Deringer, W. Zhang, P. Rausch, R. Mazzarello, R. Dronskowski, and M. Wuttig, *J. Mater. Chem. C* **3**, 9519 (2015).
- ⁶¹J. H. C. Hogg and H. H. Sutherland, *Acta Cryst.* **32**, 2689 (1976).
- ⁶²A. V. Krukau, O. A. Vydrov, A. F. Izmaylov, and G. E. Scuseria, *J. Chem. Phys.* **125**, 224106 (2006).
- ⁶³L.-M. Peng, S. L. Dudarev, and M. J. Whelan, *High Energy Electron Diffraction and Microscopy* (Oxford University Press, Oxford, 2004).
- ⁶⁴See supplementary material at <http://dx.doi.org/10.1063/1.4950817> for further details on the structural properties of InSb and In₃SbTe₂.